

Lepton number violation at the LHC with Leptoquarks and Diquarks

Hiroaki SUGIYAMA
(Maskawa Inst., Kyoto Sangyo Univ.)

- Contents
- Introduction, Motivation
 - The Model - “colored Zee-Babu model” -
 - Lepton Number Violation at the LHC
 - Summary

based on ‘M. Kohda, HS, K. Tsumura, PLB718, 1436 (2013)’

Introduction -Neutrino Oscillation-

Neutrino masses, mixings, and oscillations

Massive neutrinos can be mixed

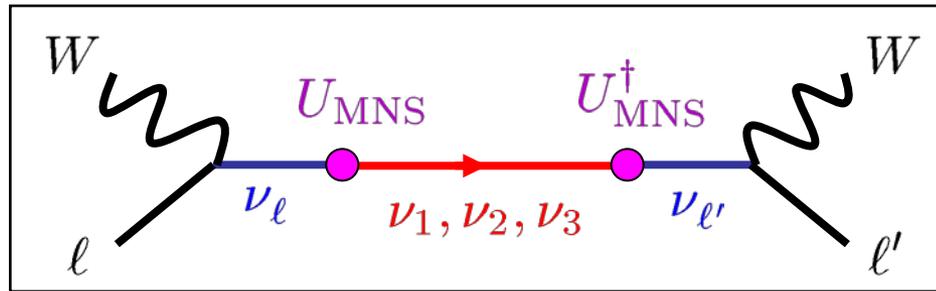
$$\nu_\ell = \sum_i (U_{\text{MNS}})_{\ell i} \nu_i$$

ν_ℓ : **flavor** eigenstates (weak interaction)
 ν_i : **mass** eigenstates (propagation)
 U_{MNS} : Maki-Nakagawa-Sakata matrix (**mixing**)
 (quark sector : Cabibbo-Kobayashi-Maskawa matrix)

Flavor transitions (oscillations) are possible

$$P(\nu_\ell \rightarrow \nu_{\ell'}) = \left| \sum_i (U_{\text{MNS}})_{\ell i} \exp\left(i \frac{m_i^2 L}{2E}\right) (U_{\text{MNS}}^\dagger)_{i \ell'} \right|^2$$

m_i : **masses**
 L : **distance**
 E : **energy**

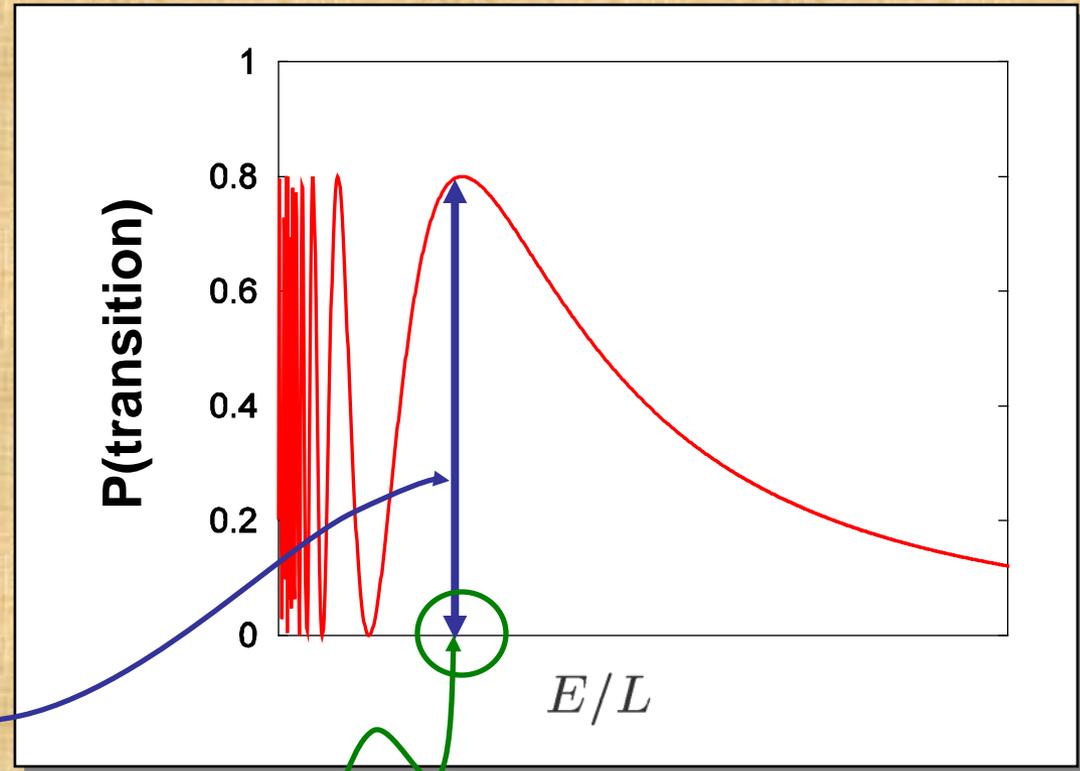


Two Neutrino Case (good approximation)

$$U_{\text{MNS}} \equiv \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$$

$$P = \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E} \right)$$

accuracy for P
 \simeq accuracy for $\sin^2 2\theta$



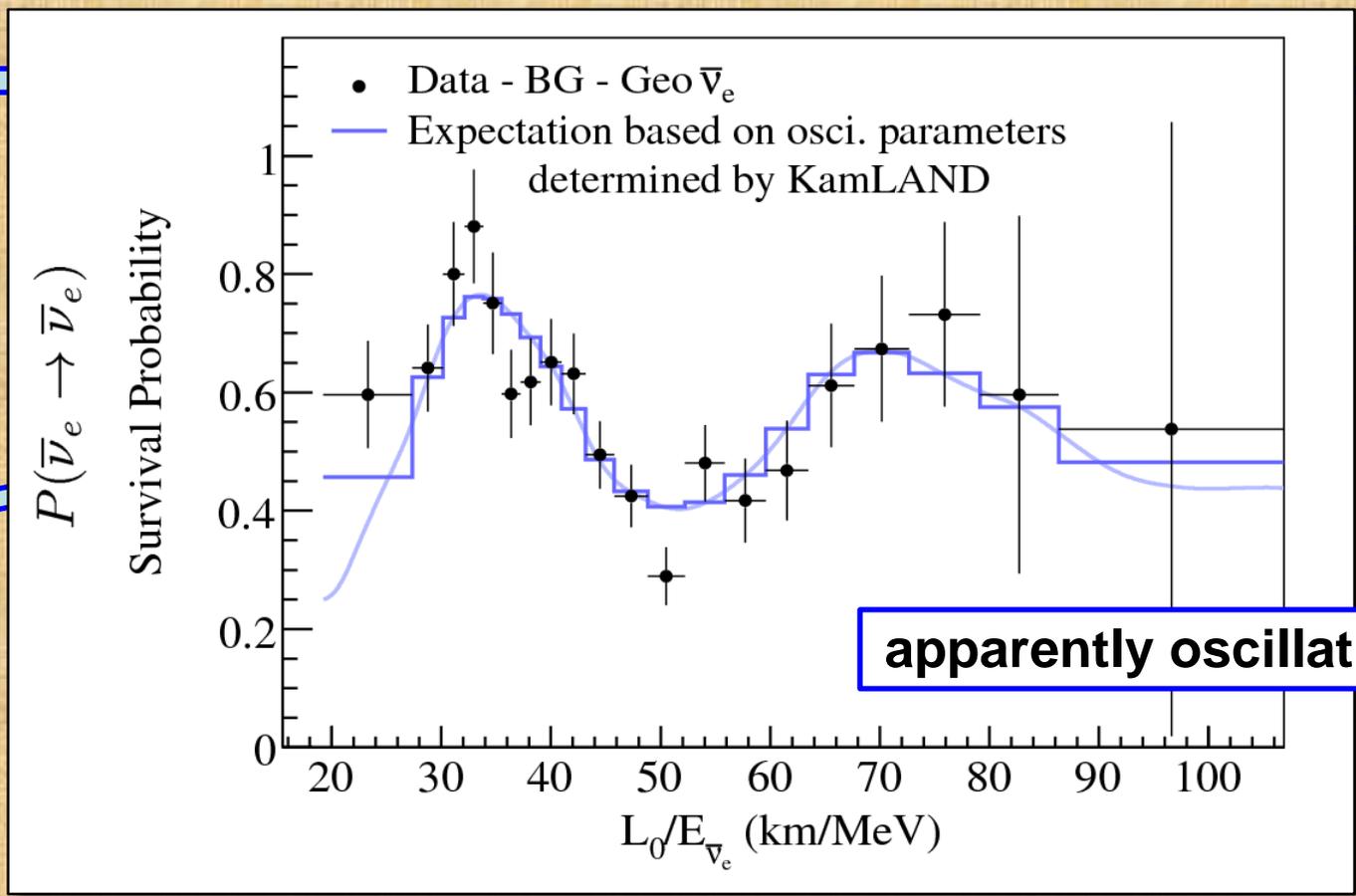
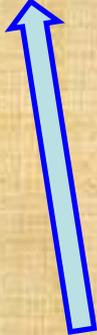
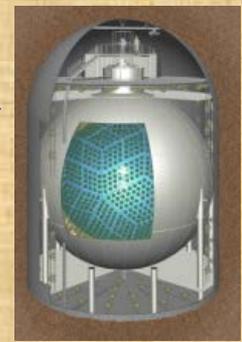
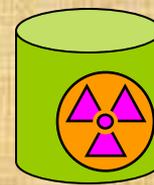
first oscillation maximum : $\frac{\Delta m^2 L}{4E} = \frac{\pi}{2}$

$$\frac{\Delta m^2 L}{4E} = 1.27 \frac{\Delta m^2 (\text{eV}^2) L(\text{m})}{E(\text{MeV})}$$

good set up (E, L) of experiments
 to obtain $\sin^2 2\theta$ and Δm^2

e.g., Measurement in KamLAND experiment

55 Japanese nuclear power reactors $\bar{\nu}_e$ Kamioka mine



S. Abe *et al.*, PRL100, 221803

We have evidence of oscillations \longrightarrow

Neutrino masses are necessary

Current knowledge on neutrino masses and mixings

$$\theta_{23} \cong 45^\circ$$

$$\theta_{13} \simeq 9^\circ$$

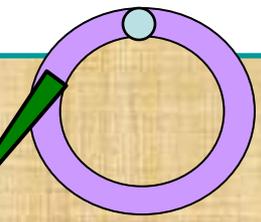
$$\delta ?$$

$$\theta_{12} \simeq 33^\circ$$

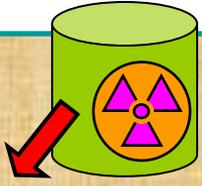
$$U_{MNS} \simeq \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0.71 & 0.71 \\ 0 & -0.71 & 0.71 \end{pmatrix} \begin{pmatrix} 0.99 & 0 & 0.15 \\ 0 & 1 & 0 \\ 0.15 & 0 & 0.99 \end{pmatrix} \begin{pmatrix} 0.83 & 0.55 & 0 \\ -0.55 & 0.83 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$



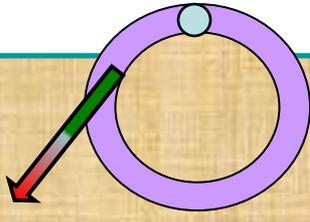
atmospheric



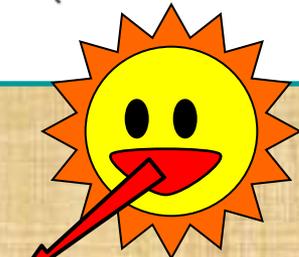
accelerator



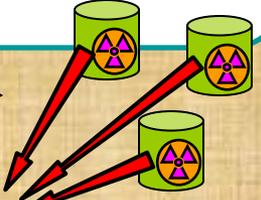
reactor



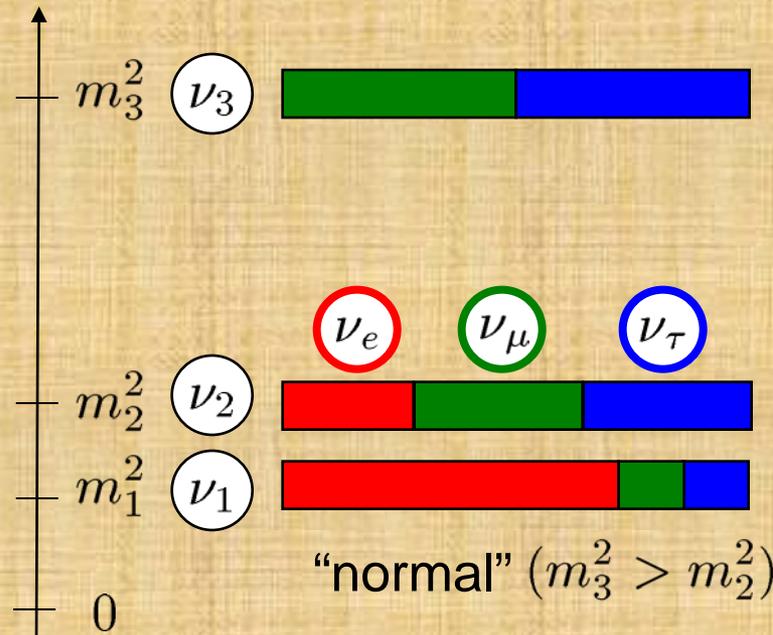
T2K



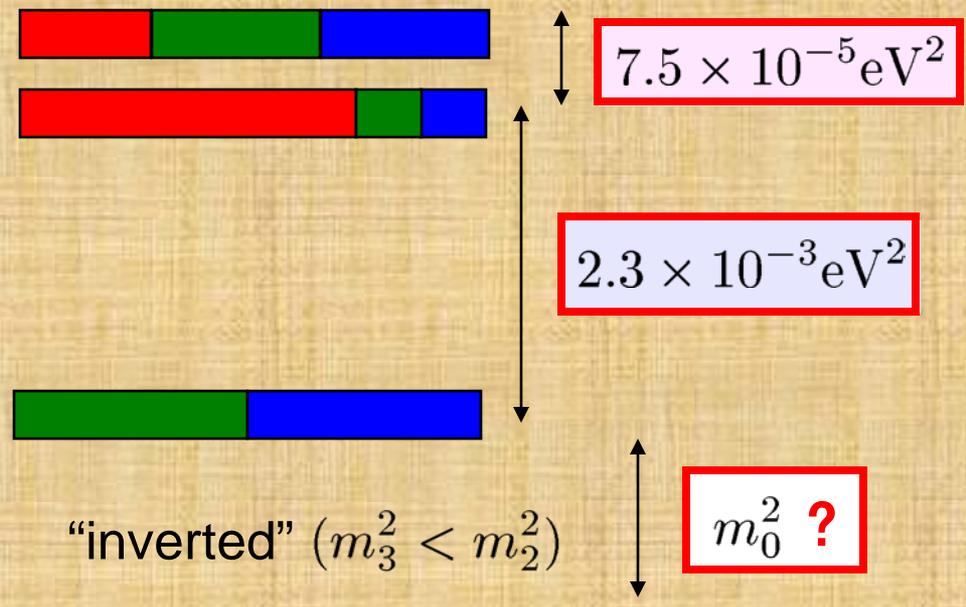
solar



KamLAND



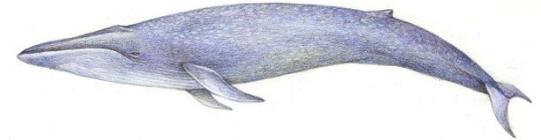
or



Introduction -Neutrino Mass-

Neutrino masses are extremely smaller than other fermion masses.

neutrino $\lesssim 1 \text{ eV}$ electron = 0.5 MeV tau = 1.8 GeV top = 172 GeV



1 MeV "≈" 1 kg

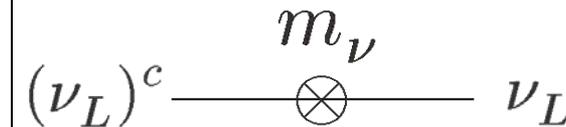
→ neutrino-specific mechanism to generate their masses ?

c.f. $m_\nu = y_\nu \frac{v_{\text{SM}}}{\sqrt{2}} \Rightarrow y_\nu \sim 10^{-12}$ **for** $m_\nu \sim 0.1 \text{ eV}$
"Unnatural"

Neutrino-specific mass term



Majorana : $\frac{1}{2} m_\nu \overline{(\nu_L)^c} \nu_L$



$Q_{EM} : 0 + 0 = 0$ **Allowed only for neutrinos**

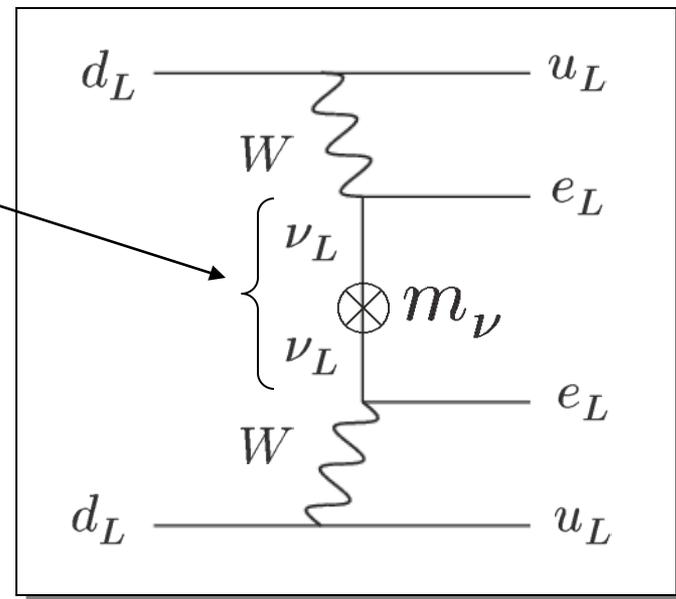
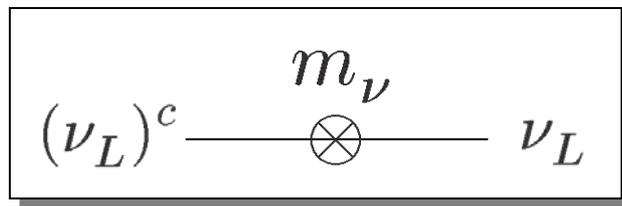
$L\# : 1 + 1 = 2$ **Lepton number violation**

Majorana mass & L#V processes



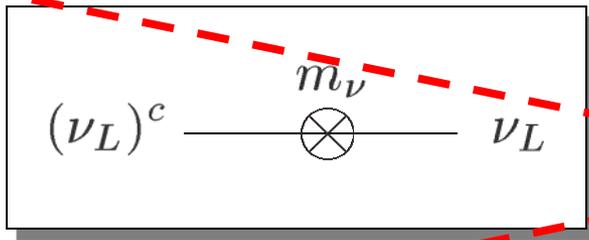
Majorana neutrino \Rightarrow L#V process
(tiny mass) (tiny rate)

e.g., Neutrinoless double beta decay

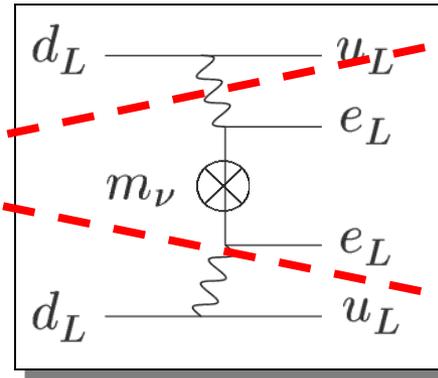


Motivation

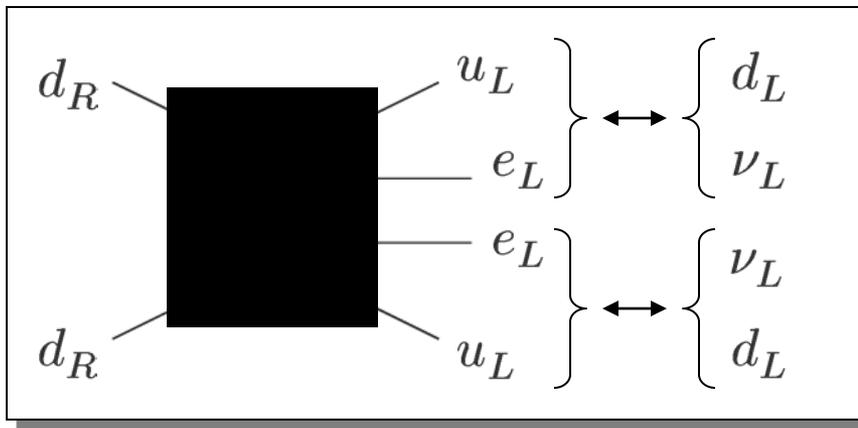
Input : Small m_ν



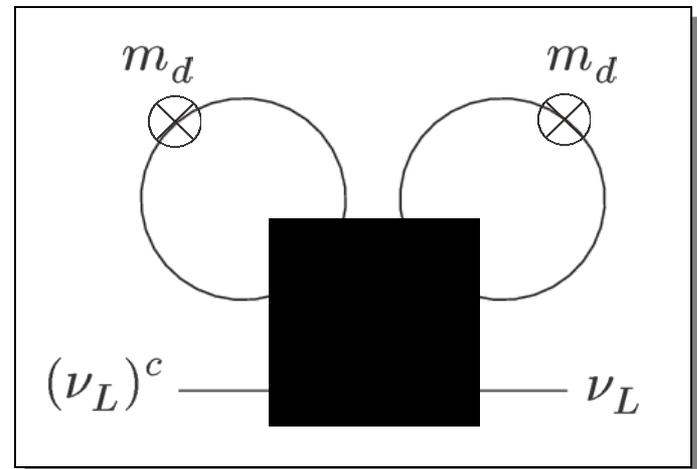
Output : Small rate of L#V



Input : **Unsuppressed** L#V



Output : **Suppressed** m_ν



Black box : TeV-scale particles

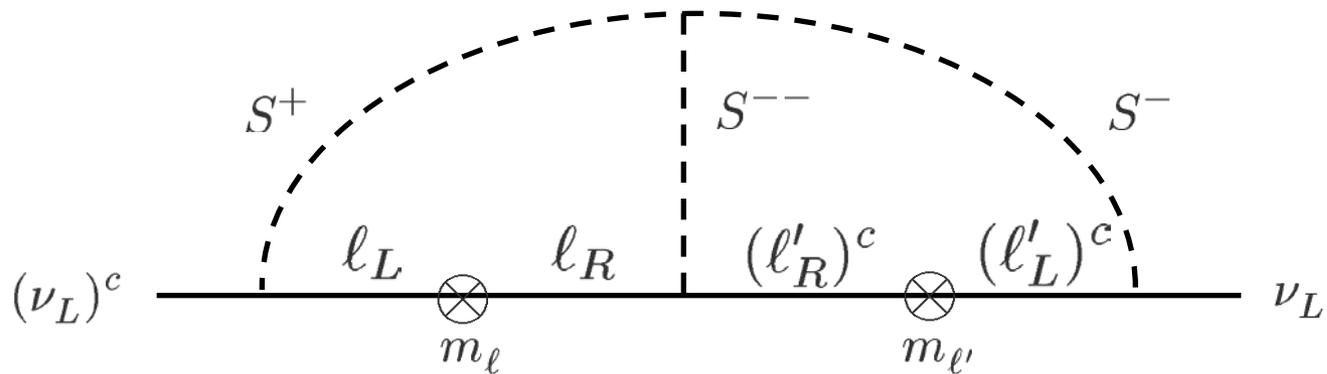
No m_ν

Two-Loop Neutrino Mass

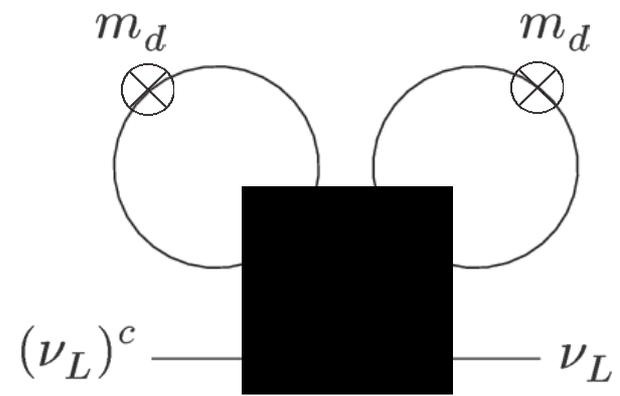
Zee-Babu Model

A. Zee, NPB264, 99 (1986)

K.S. Babu, PLB203, 132 (1988)



colored version



two colored loops

Lepton number violation at the LHC with Leptoquarks and Diquarks

Hiroaki SUGIYAMA
(Maskawa Inst., Kyoto Sangyo Univ.)

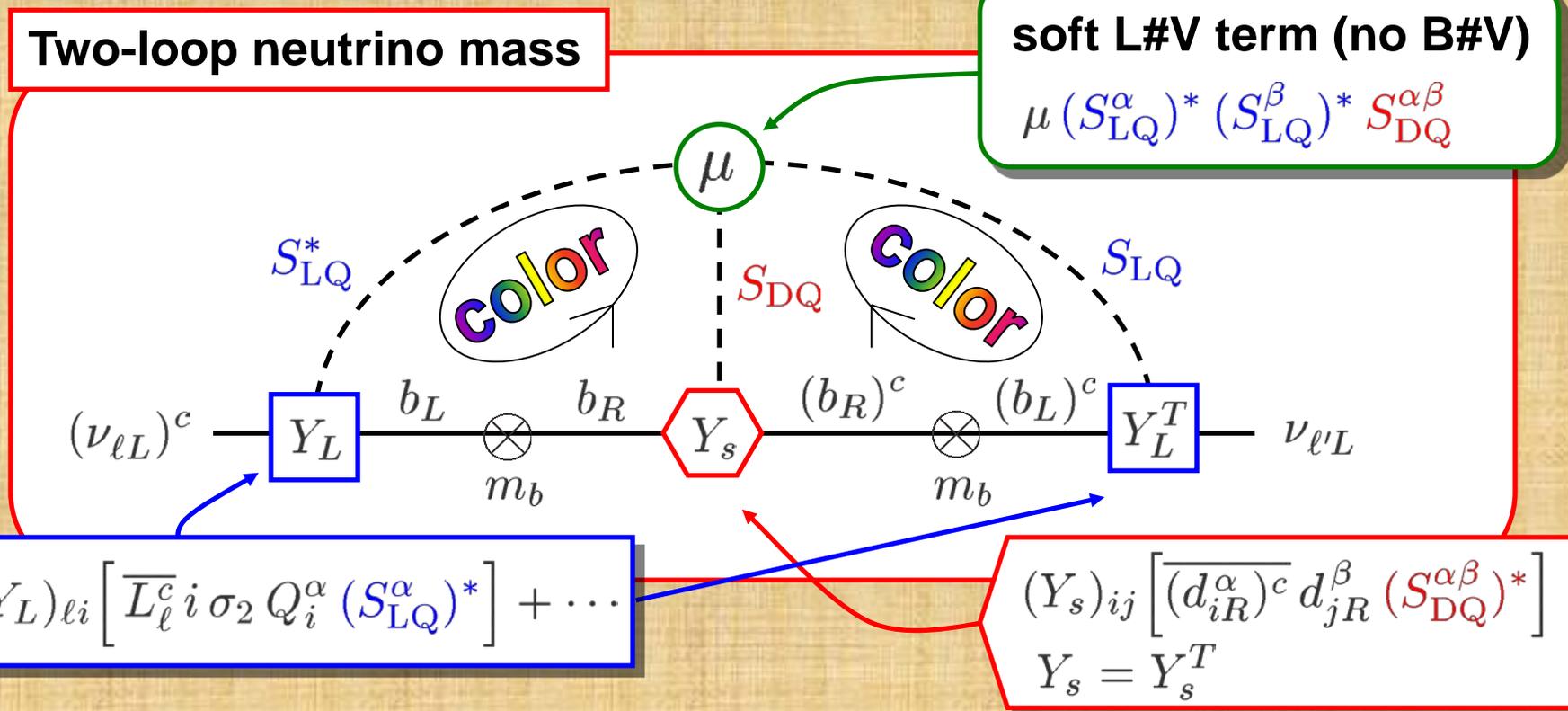
- Contents
- Introduction, Motivation
 - **The Model - “colored Zee-Babu model” -**
 - Lepton Number Violation at the LHC
 - Summary

based on ‘M. Kohda, HS, K. Tsumura, PLB718, 1436 (2013)’

The Model - colored Zee-Babu Model -

Briefly mentioned in 'K.S. Babu and C.N. Leung, NPB619, 667 (2001)'

		$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$B\#$	$L\#$
Scalar Leptoquark	S_{LQ}	<u>3</u>	<u>1</u>	$-1/3$	$1/3$	1
Scalar Diquark	S_{DQ}	<u>6</u>	<u>1</u>	$-2/3$	$2/3$	0



A Benchmark Point

$$\text{LQ Yukawa : } Y_L = \begin{matrix} e(\nu_e) \\ \mu(\nu_\mu) \\ \tau(\nu_\tau) \end{matrix} \begin{pmatrix} u(d) & c(s) & t(b) \\ 8.1 \times 10^{-5} & 3.5 \times 10^{-2} & -5.6 \times 10^{-3} \\ -4.9 \times 10^{-5} & 4.5 \times 10^{-2} & 3.5 \times 10^{-2} \\ 3.1 \times 10^{-5} & -1.9 \times 10^{-2} & 7.2 \times 10^{-2} \end{pmatrix}$$

$$\text{DQ Yukawa : } Y_s = \begin{matrix} d & s & b \\ d & s & b \\ s & b & d \\ b & d & s \end{matrix} \begin{pmatrix} 1.0 \times 10^{-1} & 0 & 0 \\ 0 & 0 & -1.7 \times 10^{-2} \\ 0 & -1.7 \times 10^{-2} & -5.9 \times 10^{-4} \end{pmatrix}$$

$$\text{Scale : } \mu = 1 \text{ TeV} \quad m_{\text{LQ}} = 1 \text{ TeV} \quad m_{\text{DQ}} = 4 \text{ TeV}$$



satisfy constraints (couplings, masses)

$$\sin^2 2\theta_{23} = 1 \quad \sin^2 2\theta_{13} = 0.1 \quad \sin^2 2\theta_{12} = 0.87$$

$$\delta = 0 \quad \alpha_{21} = 0 \quad \alpha_{31} = \pi$$

$$m_1 \simeq 0 \quad \Delta m_{21}^2 = 7.6 \times 10^{-5} \text{ eV}^2 \quad \Delta m_{31}^2 = +2.4 \times 10^{-3} \text{ eV}^2$$

agree with neutrino oscillation data

Lepton number violation at the LHC with Leptoquarks and Diquarks

Hiroaki SUGIYAMA
(Maskawa Inst., Kyoto Sangyo Univ.)

- Contents
- Introduction, Motivation
 - The Model - “colored Zee-Babu model” -
 - **Lepton Number Violation at the LHC**
 - Summary

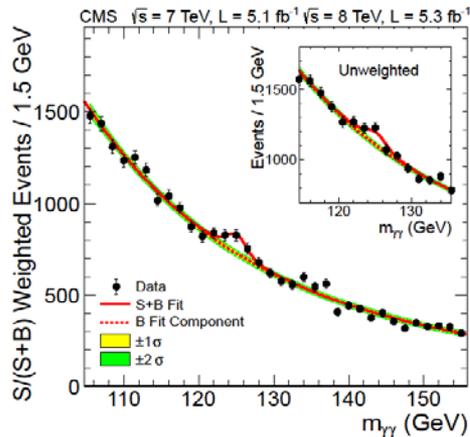
based on ‘M. Kohda, HS, K. Tsumura, PLB718, 1436 (2013)’

Large Hadron Collider

Higgs at CMS



4 Apr. 2008

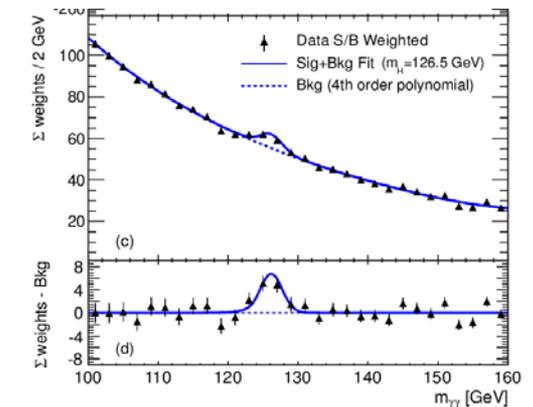


4 Jul. 2012

Higgs at ATLAS



4 Apr. 2008



4 Jul. 2012

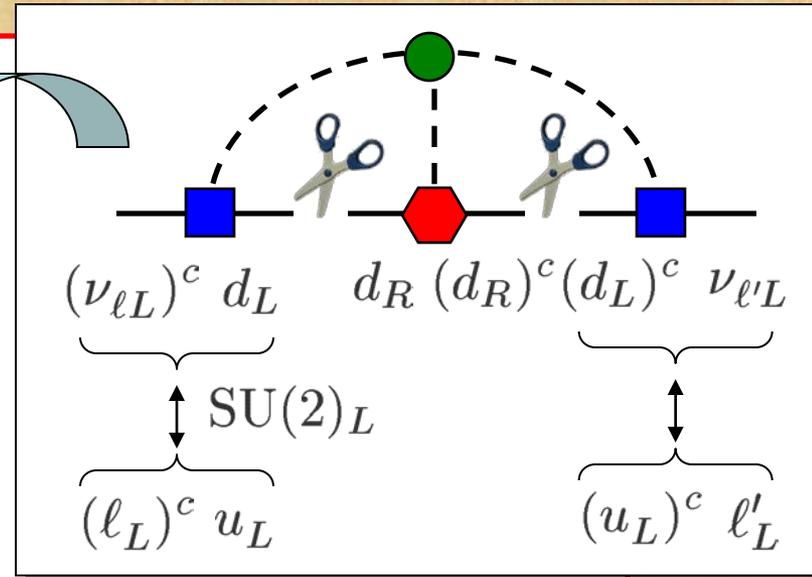
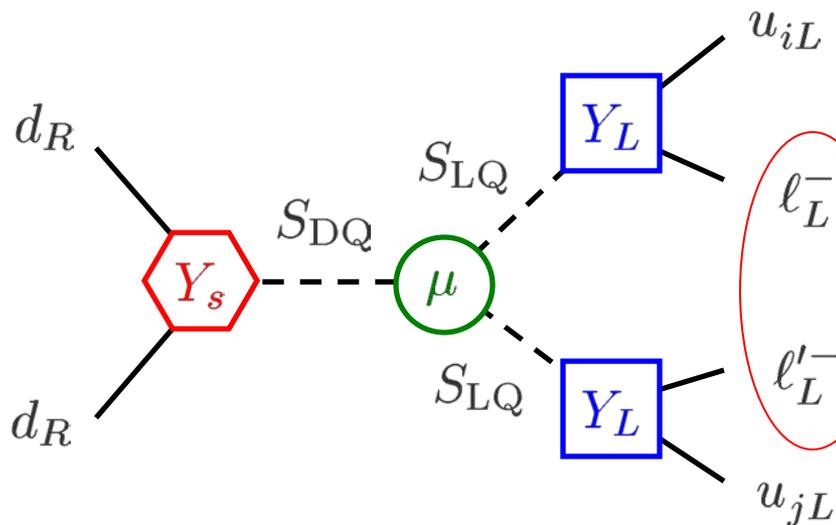
pp collider at $\sqrt{s} = 7, 8, 14 \text{ TeV}$ (cf. Tevatron: $p\bar{p}$ at $\sqrt{s} = 1.96 \text{ TeV}$)

26.7km ring (cf. 26.4km loop subway in Nagoya, Japan)
 (cf. 21.7km loop line in Osaka, Japan)



L#V Process at the LHC

$pp \rightarrow \ell^- \ell'^- jj$ **without missing**



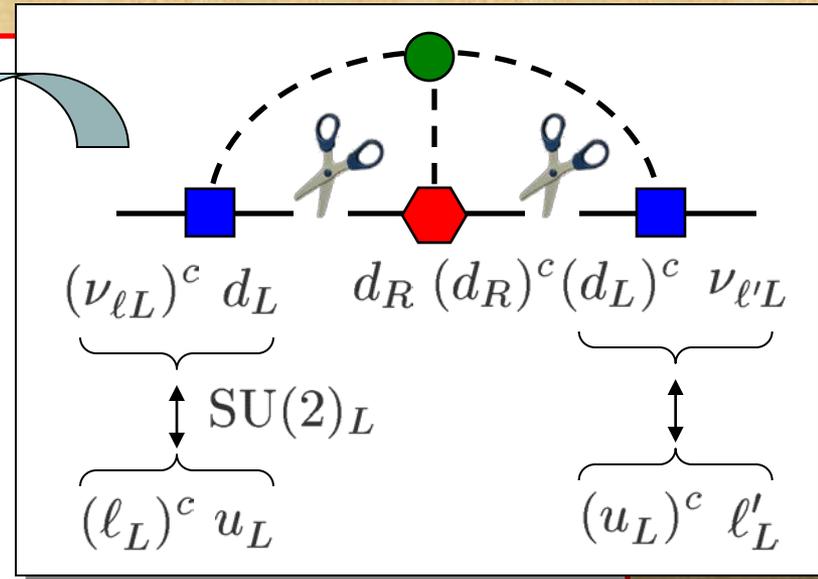
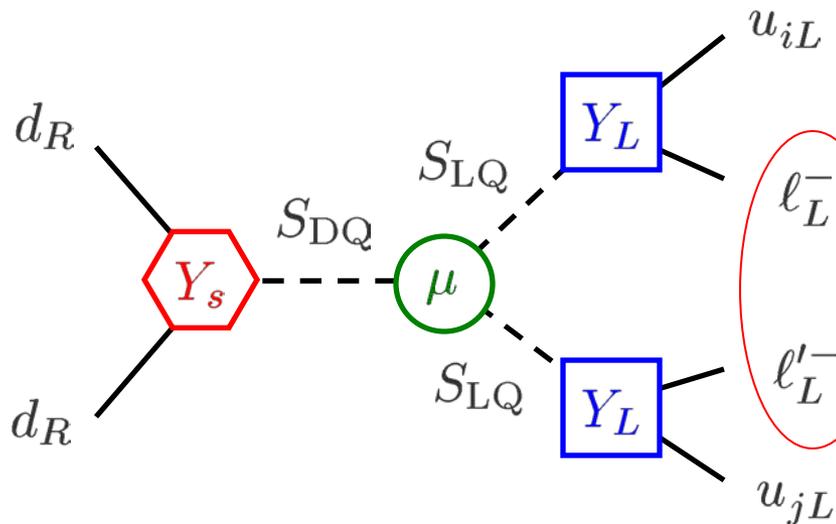
No missing energy \Rightarrow **No missing L#** ($\nu, \bar{\nu}, DM, \text{etc.}$)

\Rightarrow **Definite total L# of final states**



Evidence for L#V

$pp \rightarrow \ell^- \ell'^- jj$ **without missing**

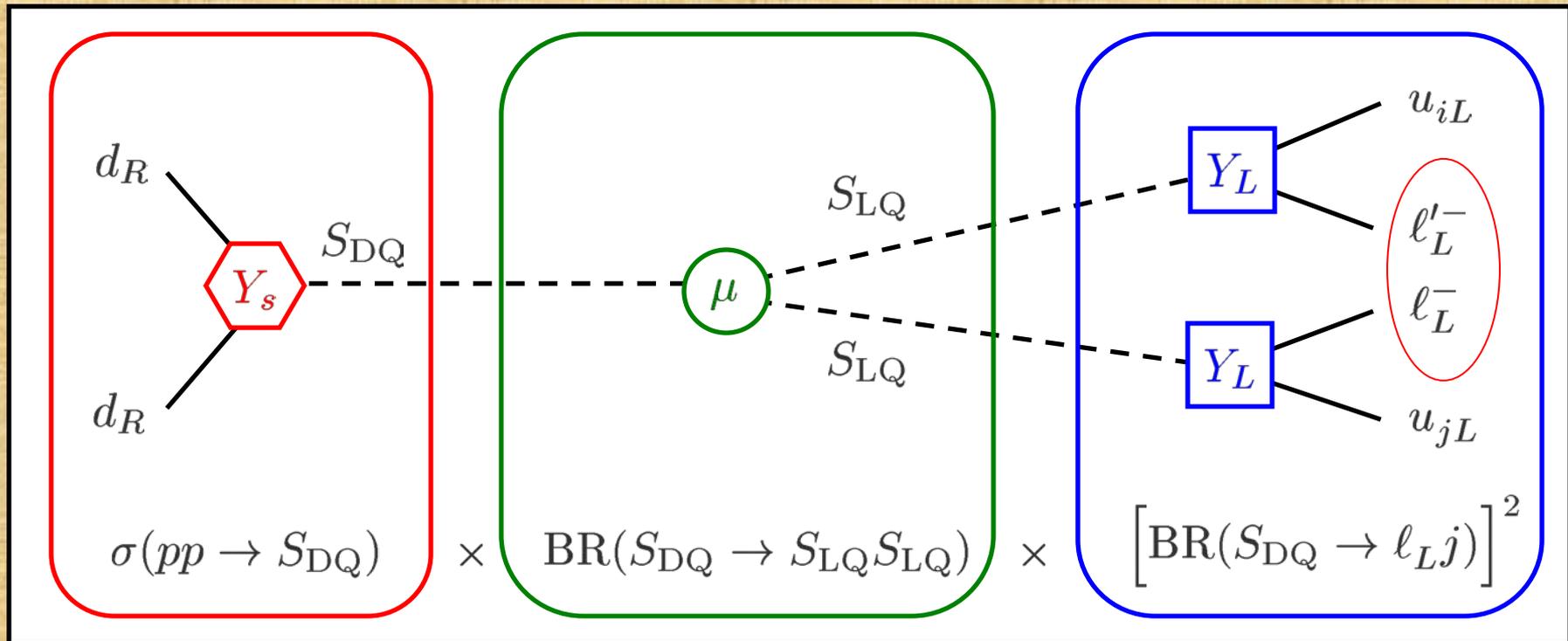


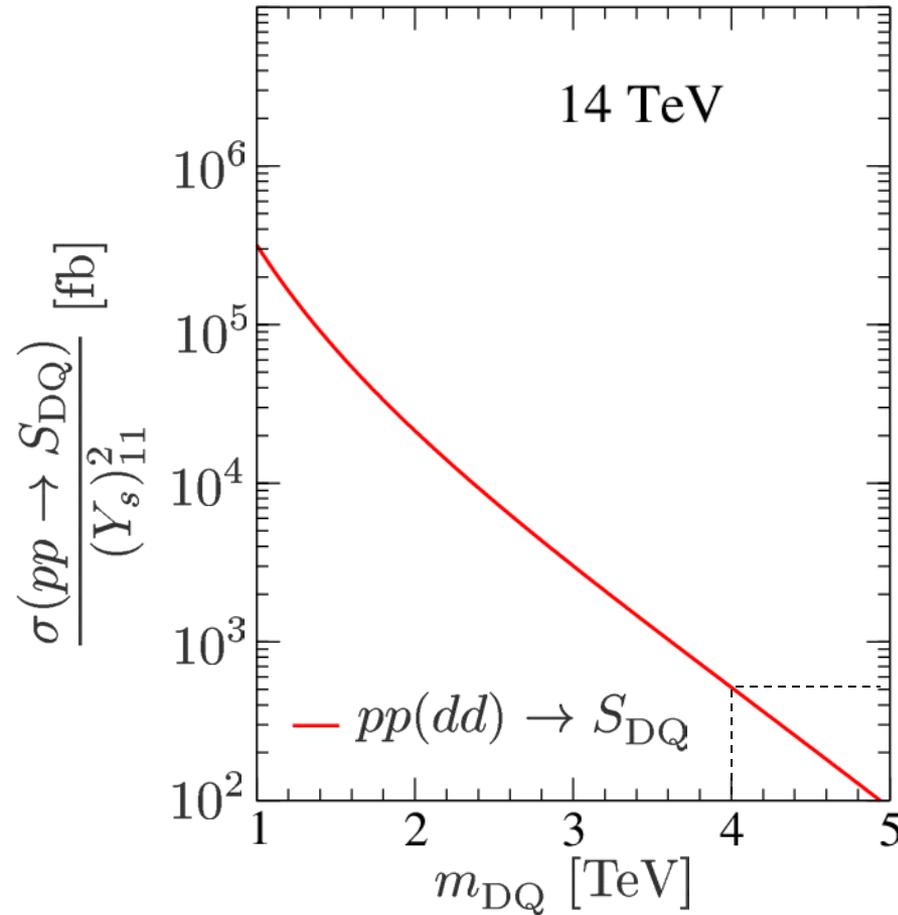
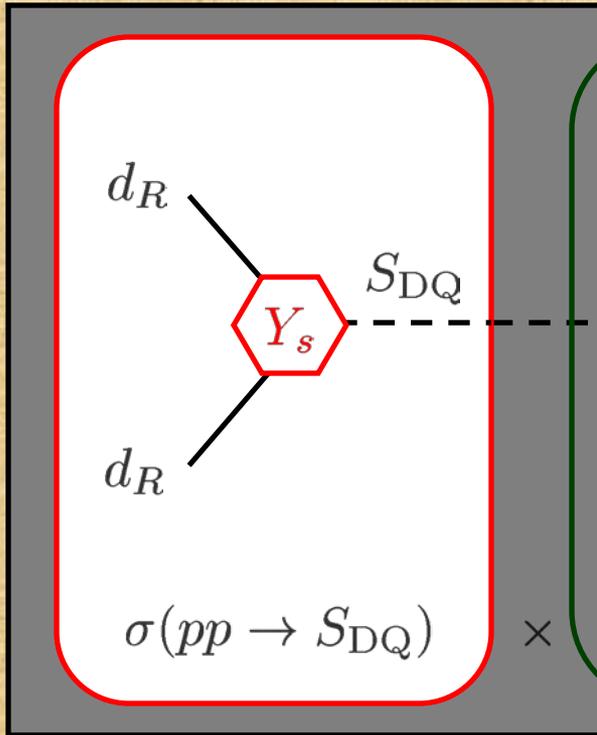
L#V \Rightarrow **No SM process in principle**

Hard ℓ_L^- (\sim TeV) \Rightarrow **No mimic event in SM**



Clear evidence for **L#V**

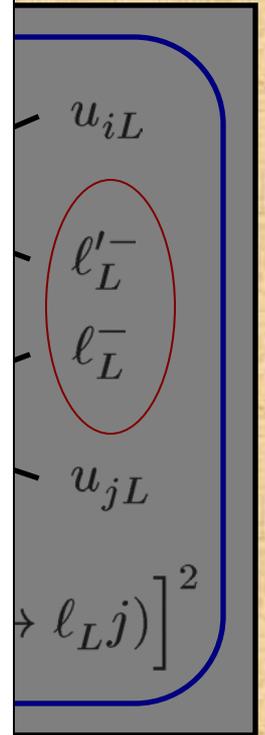


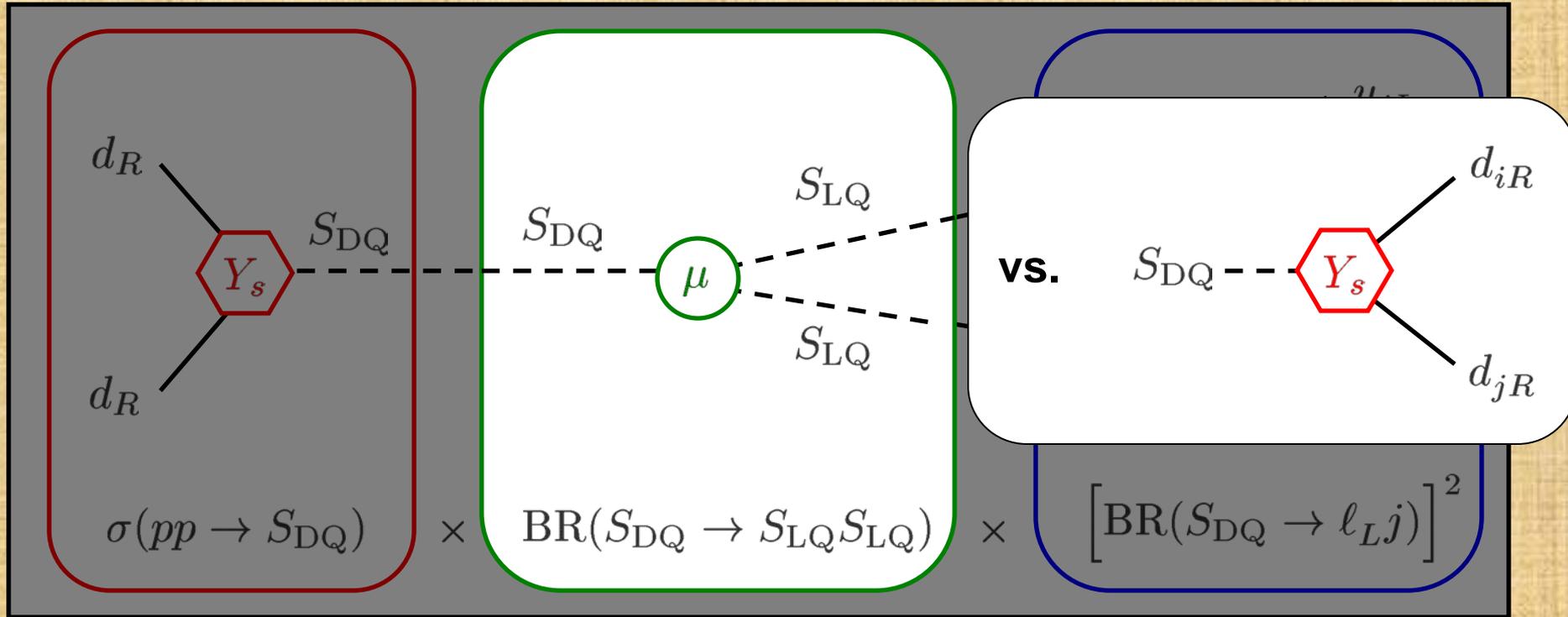


T. Han *et al.*, JHEP **1012**, 085 (2010)

$$\sigma(pp \rightarrow S_{DQ}) \simeq 5 \text{ fb at } \sqrt{s} = 14 \text{ TeV}$$

$$\text{for } (Y_s)_{11} = 0.1, m_{DQ} = 4 \text{ TeV}$$





For fixed μ

{ **Large** $Y_s \Rightarrow$ **Good for** $\sigma(pp \rightarrow S_{DQ})$ & **Bad for** $\text{BR}(S_{DQ} \rightarrow S_{LQ} S_{LQ})$
 { **Small** $Y_s \Rightarrow$ **Bad for** $\sigma(pp \rightarrow S_{DQ})$ & **Good for** $\text{BR}(S_{DQ} \rightarrow S_{LQ} S_{LQ})$

$$\frac{\sum_{i,j} \Gamma(S_{DQ} \rightarrow d_i d_j)}{\Gamma(S_{DQ} \rightarrow S_{LQ} S_{LQ})} \simeq \frac{m_{DQ}^2 \text{tr}(Y_s Y_s^\dagger)}{\mu^2} = \mathcal{O}(0.1) - \mathcal{O}(1) \quad \text{is preferred}$$

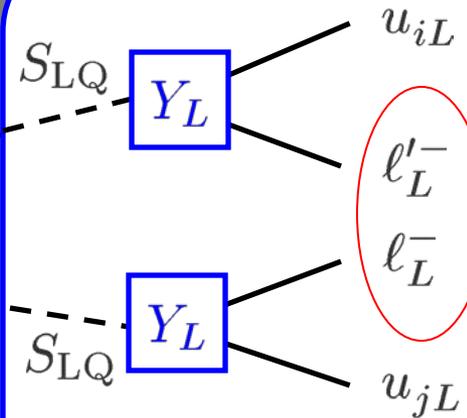
Benchmark point $\Rightarrow 0.20 \Rightarrow \text{BR}(S_{DQ} \rightarrow S_{LQ} S_{LQ}) = 84\%$

$\Gamma(S_{LQ} \rightarrow \ell_L u_{iL}) \propto |(Y_L)_{li}|^2$ is small

BUT $\Gamma_{\text{tot}} \propto \text{tr}(Y_L Y_L^\dagger)$ is also small.



Sizable $\text{BR}(S_{DQ} \rightarrow \ell_L j)$



$\sigma(pp \rightarrow S_{DQ})$

\times

$\text{BR}(S_{DQ} \rightarrow S_{LQ} S_{LQ})$

\times

$[\text{BR}(S_{DQ} \rightarrow \ell_L j)]^2$

@ Benchmark point

$$\text{BR} \simeq \begin{pmatrix} e(\nu_e) \\ \mu(\nu_\mu) \\ \tau(\nu_\tau) \end{pmatrix} \begin{pmatrix} u(d) & c(s) & t(b) \\ 3.3 \times 10^{-7} & 6.0 \times 10^{-2} & 1.6 \times 10^{-3} \\ 1.2 \times 10^{-7} & 1.0 \times 10^{-1} & 6.2 \times 10^{-2} \\ 4.7 \times 10^{-6} & 1.9 \times 10^{-2} & 2.6 \times 10^{-1} \end{pmatrix}$$

16% ℓj w/o missing

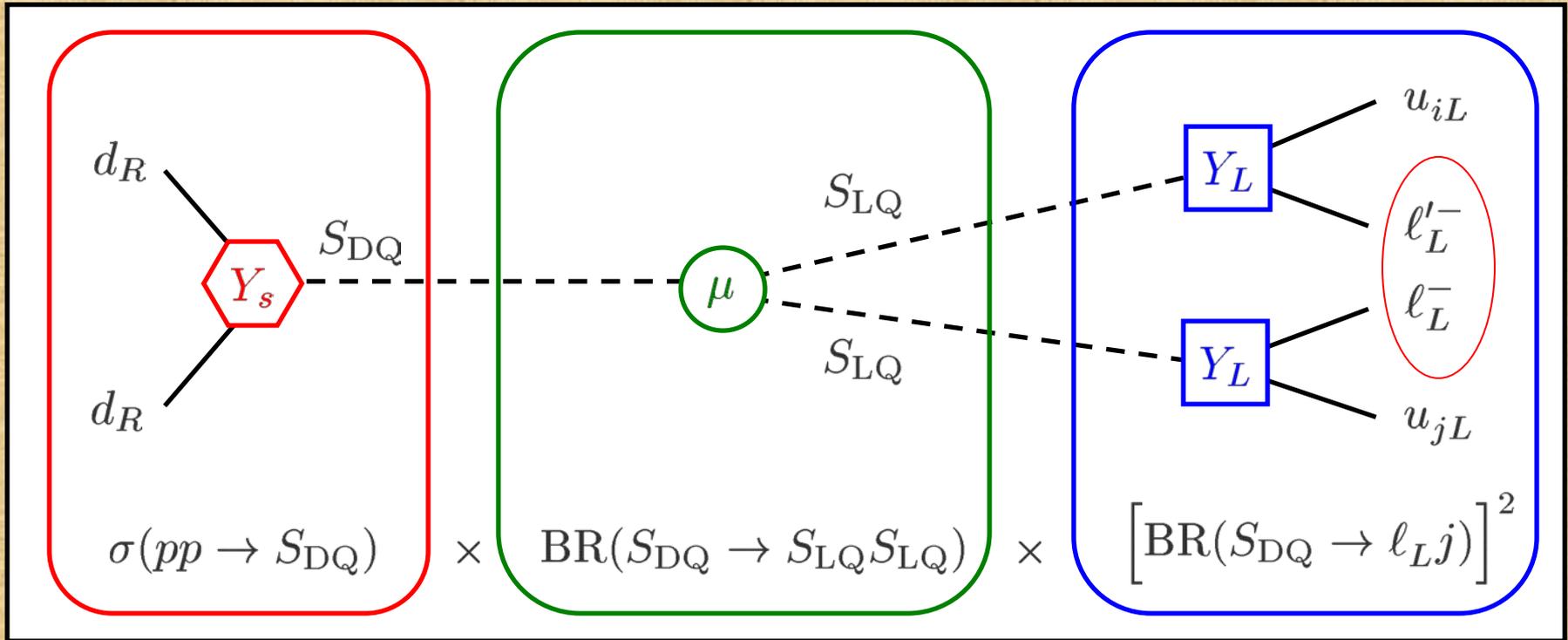
28% τ w/ missing

(50% $\ell u_i + 50\%$ $\nu_\ell d_i$)

6% t

$\rightarrow \times 68\%$ $b j j$

w/o missing



Benchmark point & LHC with $\sqrt{s} = 14$ TeV

$\sigma(pp \rightarrow \ell^- \ell'^- + \text{jets} + \text{no missing})$

$$\simeq 5 \text{ [fb]} \times 84\% \times (16\% + 6\% \times 68\%)^2 \simeq 0.17 \text{ [fb]}$$

ℓj

$\ell b j j$

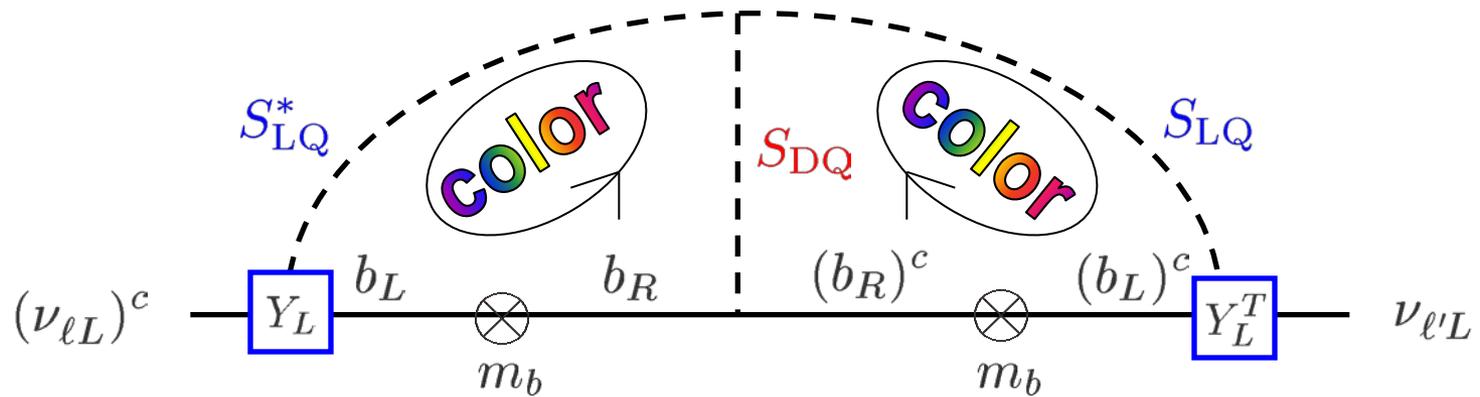
$$\begin{cases} \ell \ell' j j \text{ (0.11 [fb])} \\ \ell \ell' b j j j \\ \ell \ell' b b j j j j \end{cases}$$

Summary



Colored Zee-Babu Model with Leptoquark and Diquark

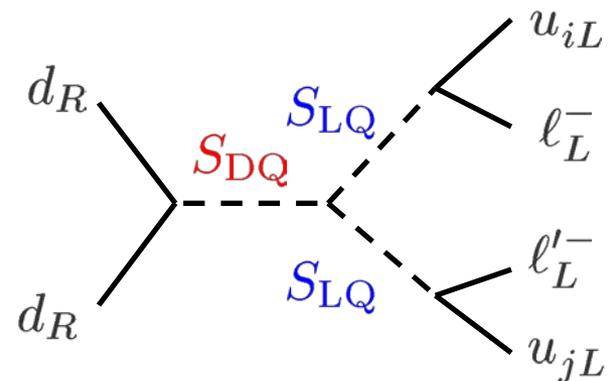
Suppressed neutrino mass (two-loop, $(m_b/m_{DQ})^2, Y_L^2$)



Unsuppressed L#V process at the LHC

$pp \rightarrow \ell^- \ell'^- jj$ **without missing**

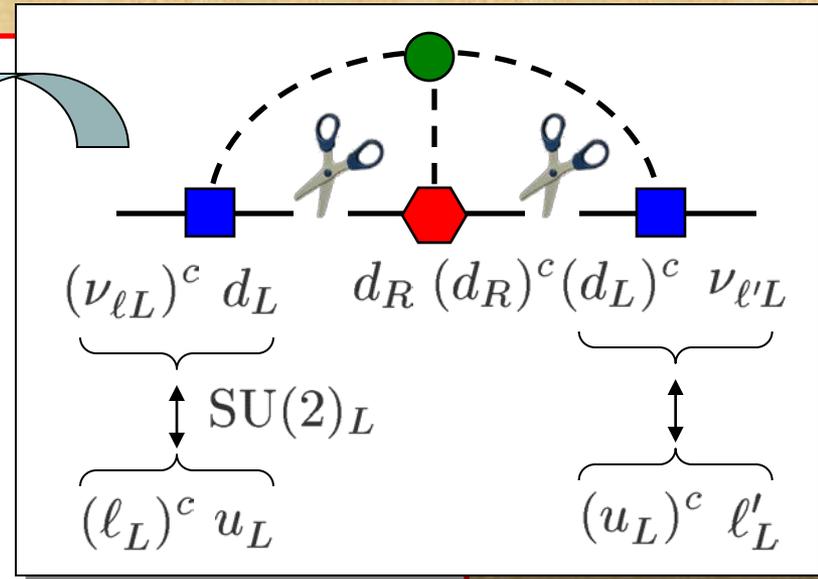
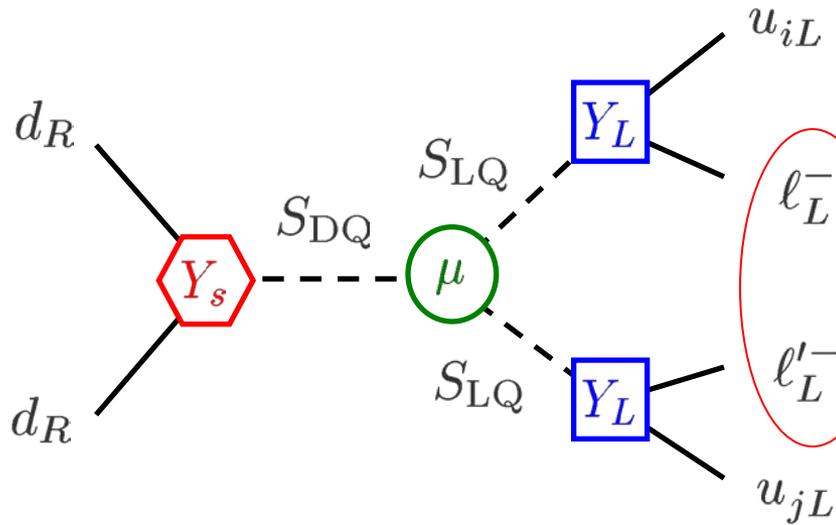
$$\begin{aligned} & \sigma(pp \rightarrow S_{DQ}) \\ & \times \text{BR}(S_{DQ} \rightarrow S_{LQ} S_{LQ}) \\ & \times \left[\text{BR}(S_{DQ} \rightarrow \ell_L j) \right]^2 \end{aligned}$$



Backup

L#V Process at the LHC

$pp \rightarrow \ell^- \ell'^- jj$ **without missing**



$\sim 1 \text{ fb}$ **at** $\sqrt{s} = 7 \text{ TeV}$
for $Y_s \sim 0.1, m_{DQ} \simeq 4 \text{ TeV}$

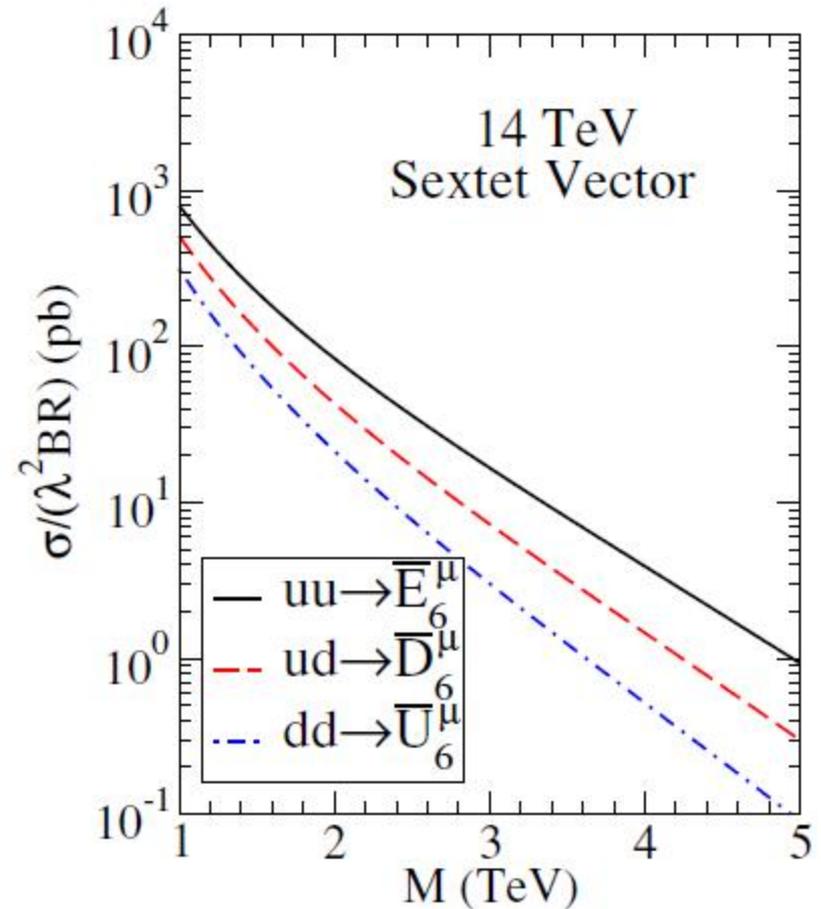
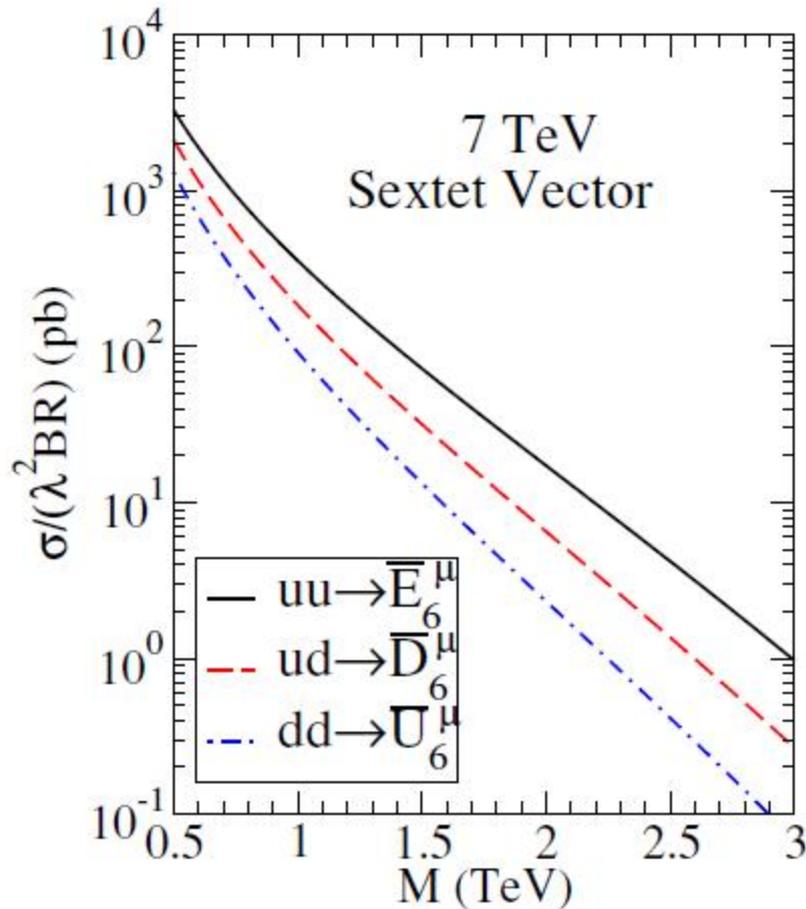
$[\mathcal{O}(0.1)]^2$ **even for** $Y_L \ll 1$

$$\sigma(pp \rightarrow S_{DQ}) \times \text{BR}(S_{DQ} \rightarrow S_{LQ} S_{LQ}) \times [\text{BR}(S_{DQ} \rightarrow \ell_L j)]^2$$

$$\mathcal{O}(1) \text{ for } \frac{\sum_{i,j} \Gamma(S_{DQ} \rightarrow d_i d_j)}{\Gamma(S_{DQ} \rightarrow S_{LQ} S_{LQ})} \simeq \frac{m_{DQ}^2 \text{tr}(Y_s Y_s^\dagger)}{\mu^2} \lesssim 1$$

Production Cross Section

$$\sigma(\text{scalar}) = \frac{1}{2} \sigma(\text{vector})$$



Bounds on Masses

Leptoquark mass (for $\text{BR}(S_{LQ} \rightarrow \ell u) = \text{BR}(S_{LQ} \rightarrow \nu d) = 50\%$)

CMS : $\sqrt{s} = 7 \text{ TeV}, 5.0 \text{ fb}^{-1}$ PRD86, 052013 (2012)

$$pp \rightarrow S_{LQ} S_{LQ}^* \rightarrow e\bar{e}jj, e\bar{\nu}jj \Rightarrow m_{LQ} > 640 \text{ GeV (95\%CL)}$$

$$pp \rightarrow S_{LQ} S_{LQ}^* \rightarrow \mu\bar{\mu}jj, \mu\bar{\nu}jj \Rightarrow m_{LQ} > 650 \text{ GeV (95\%CL)}$$

ATLAS : $\sqrt{s} = 7 \text{ TeV}, 1.03 \text{ fb}^{-1}$ PLB709, 158 (2012)

$$pp \rightarrow S_{LQ} S_{LQ}^* \rightarrow e\bar{e}jj, e\bar{\nu}jj \Rightarrow m_{LQ} > 607 \text{ GeV (95\%CL)}$$

$\sqrt{s} = 7 \text{ TeV}, 1.03 \text{ fb}^{-1}$ EPJC72, 2151 (2012)

$$pp \rightarrow S_{LQ} S_{LQ}^* \rightarrow \mu\bar{\mu}jj, \mu\bar{\nu}jj \Rightarrow m_{LQ} > 594 \text{ GeV (95\%CL)}$$

Diquark mass

No analysis for $Y = -2/3$ ($dd \rightarrow S_{DQ}$)

cf. CMS : $\sqrt{s} = 8 \text{ TeV}, 4.0 \text{ fb}^{-1}$ arXiv:1302.4794

$$pp \rightarrow S_{DQ} \rightarrow jj \Rightarrow m_{DQ} > 4.28 \text{ TeV (95\%CL)}$$

$$(Y = 1/3, ud \rightarrow S_{DQ})$$

Bounds on Masses

Leptoquark mass

CMS : $\sqrt{s} = 7 \text{ TeV}$, 5.0 fb^{-1} PRD86, 052013 (2012)

$$pp \rightarrow S_{LQ} S_{LQ}^* \rightarrow e\bar{e}jj, e\bar{\nu}jj \Rightarrow m_{LQ} > 640 \text{ GeV (95\%CL)}$$

$$pp \rightarrow S_{LQ} S_{LQ}^* \rightarrow \mu\bar{\mu}jj, \mu\bar{\nu}jj \Rightarrow m_{LQ} > 650 \text{ GeV (95\%CL)}$$

$$(\text{BR}(S_{LQ} \rightarrow \ell u) = \text{BR}(S_{LQ} \rightarrow \nu d) = 50 \%)$$

$$\left[\begin{array}{l} pp \rightarrow S_{LQ} S_{LQ}^* \rightarrow e\bar{e}jj \quad \Rightarrow m_{LQ} > 830 \text{ GeV (95\%CL)} \\ pp \rightarrow S_{LQ} S_{LQ}^* \rightarrow \mu\bar{\mu}jj \quad \Rightarrow m_{LQ} > 840 \text{ GeV (95\%CL)} \\ (\text{BR}(S_{LQ} \rightarrow \ell q) = 100 \%) \end{array} \right]$$

$$\left[\begin{array}{l} \sqrt{s} = 7 \text{ TeV}, 4.7 \text{ fb}^{-1} \text{ JHEP1212, 055 (2012)} \\ pp \rightarrow S_{LQ} S_{LQ}^* \rightarrow \nu\bar{\nu}j_b j_b \quad \Rightarrow m_{LQ} > 450 \text{ GeV (95\%CL)} \\ (\text{BR}(S_{LQ} \rightarrow \nu b) = 100 \%) \end{array} \right]$$

$$\left[\begin{array}{l} \sqrt{s} = 7 \text{ TeV}, 4.8 \text{ fb}^{-1} \text{ arXiv:1210.5629} \\ pp \rightarrow S_{LQ} S_{LQ}^* \rightarrow \tau\bar{\tau}j_b j_b \quad \Rightarrow m_{LQ} > 525 \text{ GeV (95\%CL)} \\ (Y = -4/3) \end{array} \right]$$

Bounds on Masses

Leptoquark mass

ATLAS : $\sqrt{s} = 7 \text{ TeV}$, 1.03 fb^{-1} PLB709, 158 (2012)

$$pp \rightarrow S_{LQ} S_{LQ}^* \rightarrow e\bar{e}jj, e\bar{\nu}jj \Rightarrow m_{LQ} > 607 \text{ GeV (95\%CL)}$$

$$(\text{BR}(S_{LQ} \rightarrow eu) = \text{BR}(S_{LQ} \rightarrow \nu d) = 50 \%)$$

$$\left[\begin{array}{l} pp \rightarrow S_{LQ} S_{LQ}^* \rightarrow e\bar{e}jj \\ (\text{BR}(S_{LQ} \rightarrow eq) = 100 \%) \end{array} \Rightarrow m_{LQ} > 660 \text{ GeV (95\%CL)} \right]$$

$\sqrt{s} = 7 \text{ TeV}$, 1.03 fb^{-1} EPJC72, 2151 (2012)

$$pp \rightarrow S_{LQ} S_{LQ}^* \rightarrow \mu\bar{\mu}jj, \mu\bar{\nu}jj \Rightarrow m_{LQ} > 594 \text{ GeV (95\%CL)}$$

$$(\text{BR}(S_{LQ} \rightarrow \mu u) = \text{BR}(S_{LQ} \rightarrow \nu d) = 50 \%)$$

$$\left[\begin{array}{l} pp \rightarrow S_{LQ} S_{LQ}^* \rightarrow \mu\bar{\mu}jj \\ (\text{BR}(S_{LQ} \rightarrow \mu q) = 100 \%) \end{array} \Rightarrow m_{LQ} > 685 \text{ GeV (95\%CL)} \right]$$

Bounds on Masses

Diquark mass

No analysis for $Y = -2/3$ ($dd \rightarrow S_{DQ}$)

cf. CMS : $\sqrt{s} = 8 \text{ TeV}$, 4.0 fb^{-1} arXiv:1302.4794

$pp \rightarrow S_{DQ} \rightarrow jj \Rightarrow m_{DQ} > 4.28 \text{ TeV (95\%CL)}$

($Y = 1/3$, $ud \rightarrow S_{DQ}$)

Constraints on New Yukawa Couplings

LQ Yukawa

M. Carpenter and S. Davidson, EPJC70, 1071 (2010)

$$\frac{(Y_L)_{e1}(Y_L^*)_{\mu 1}}{4\sqrt{2}G_F m_{LQ}^2} \times 2\sqrt{2}G_F (\bar{e}_L \gamma^\mu \mu_L) (\bar{u}_L \gamma_\mu u_L)$$

Constraint : $< 8.5 \times 10^{-7}$ (90 % C.L.) (μ - e conversion)

Benchmark : 1.2×10^{-10}

$$\frac{(Y_L)_{\ell 1}(Y_L^*)_{\ell' 2}}{4\sqrt{2}G_F m_{LQ}^2} \times 2\sqrt{2}G_F (\bar{\nu}_{\ell L} \gamma^\mu \nu_{\ell' L}) (\bar{d}_L \gamma_\mu s_L)$$

Constraint : $< 9.4 \times 10^{-6}$ (90 % C.L.) (K meson decay)

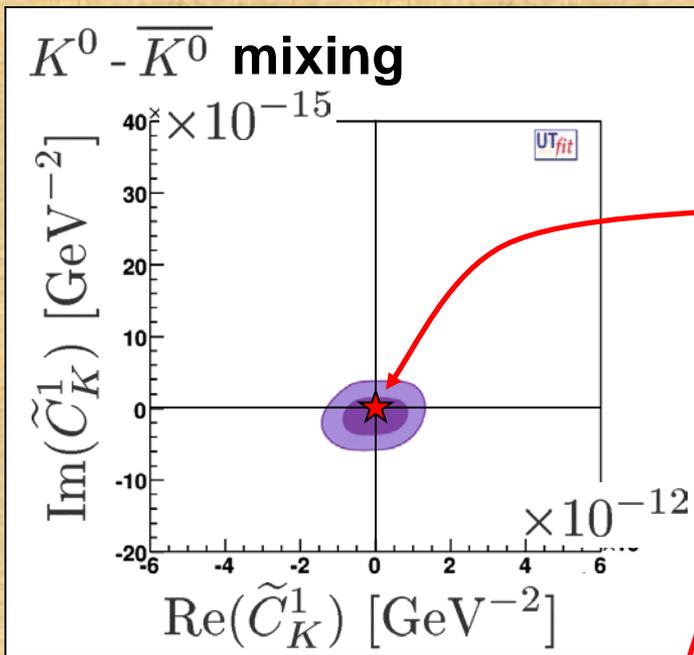
Benchmark : $\lesssim 10^{-7}$

$$\text{BR}(\mu \rightarrow e\gamma) = \frac{3\alpha_{\text{EM}}}{256\pi G_F^2 m_{LQ}^4} \left| (Y_L Y_L^\dagger)_{e\mu} \right|^2$$

Constraint : $< 2.4 \times 10^{-12}$ (90 % C.L.) MEG, PRL107, 171801 (2011)

$< 5.7 \times 10^{-13}$ (90 % C.L.) MEG, arXiv:1303.0754

Benchmark : 3.7×10^{-13}

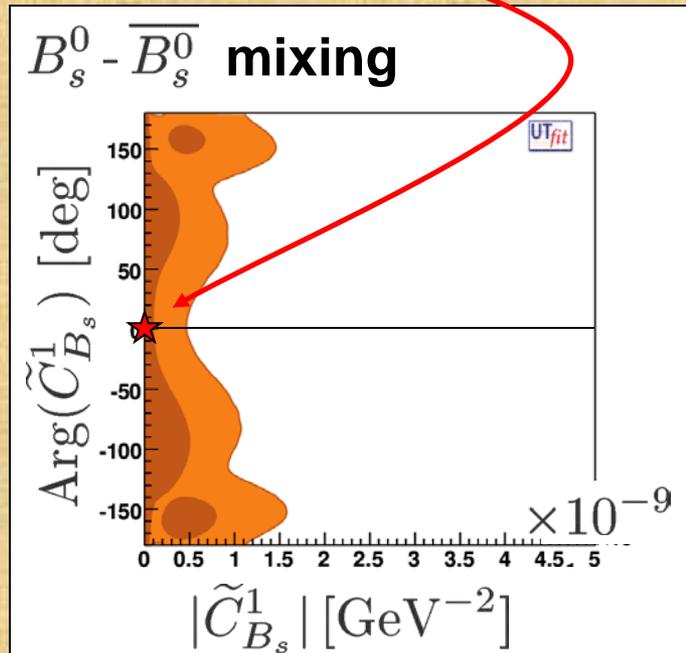
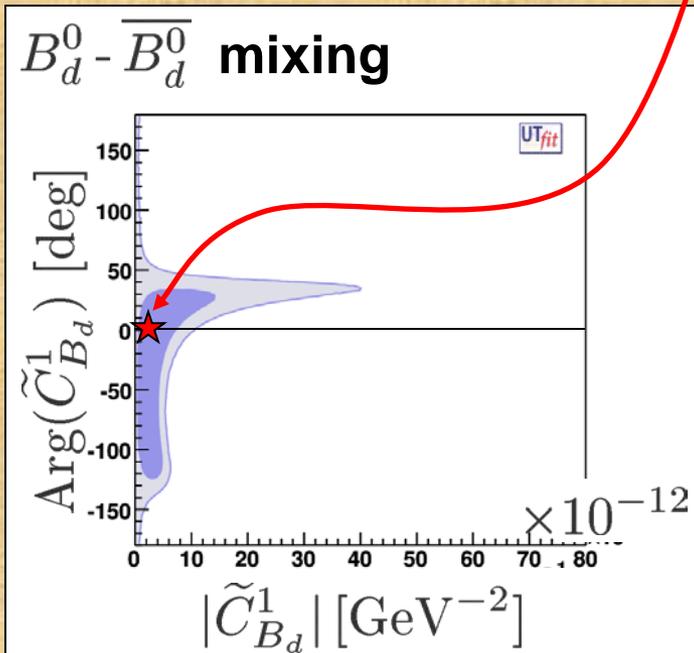


Benchmark point

$$\tilde{C}_K^1 = -\frac{(Y_s^*)_{11}(Y_s)_{22}}{2m_{DQ}^2} = 0$$

$$\tilde{C}_{B_d}^1 = -\frac{(Y_s^*)_{11}(Y_s)_{33}}{2m_{DQ}^2} = +1.9 \times 10^{-12} [\text{GeV}^{-2}]$$

$$\tilde{C}_{B_s}^1 = -\frac{(Y_s^*)_{22}(Y_s)_{33}}{2m_{DQ}^2} = 0$$



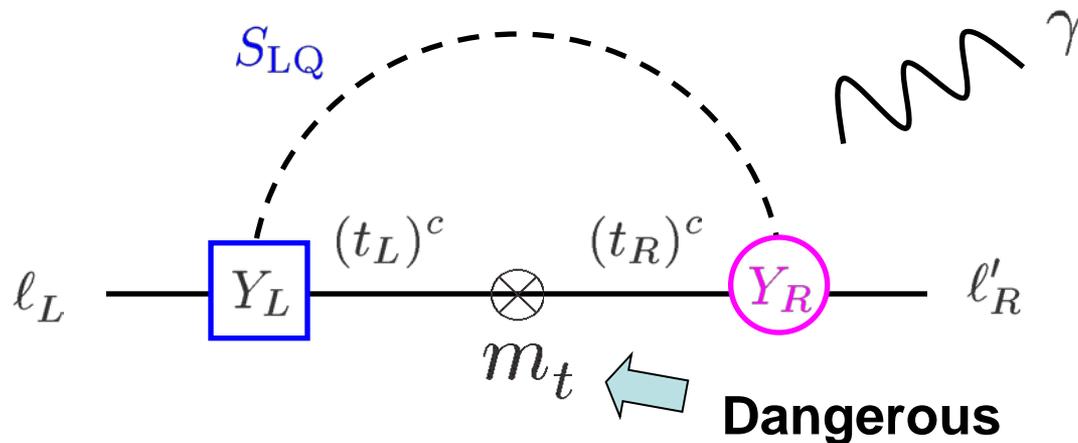
LFV

$$Q_i = \begin{pmatrix} u'_{iL} \\ d_{iL} \end{pmatrix} = \begin{pmatrix} [V_{\text{CKM}}^\dagger u_L]_i \\ d_{iL} \end{pmatrix}$$

$$\mathcal{L}_{\text{Yukawa}} = - \left\{ (Y_L)_{li} [\bar{L}_\ell^c i \sigma_2 Q_i^\alpha] + (Y_R)_{li} [(\ell_R)^c u'_{iR}^\alpha] \right\} (S_{\text{LQ}}^\alpha)^* \\ - (Y_s)_{ij} [(\bar{d}_{iR}^\alpha)^c d_{jR}^\beta (S_{\text{DQ}}^{\alpha\beta})^*] + \text{H.c.}$$

We ignore Y_R .

No $Y_R \iff$ Type-II or Type-X THDMs (u_{iR} or ℓ_R are Z_2 -odd)
or $SU(2)_L$ -triplet Leptoquark



Neutrinoless Double Beta Decay

$$(M_\nu)_{ee} \equiv \left| m_1 (U_{\text{MNS}})_{e1}^2 + m_2 e^{i\alpha_{21}} (U_{\text{MNS}})_{e2}^2 + m_3 e^{i\alpha_{31}} (U_{\text{MNS}})_{e3}^2 \right|$$
$$= 1.5 \times 10^{-3} \text{ eV @ Benchmark point}$$